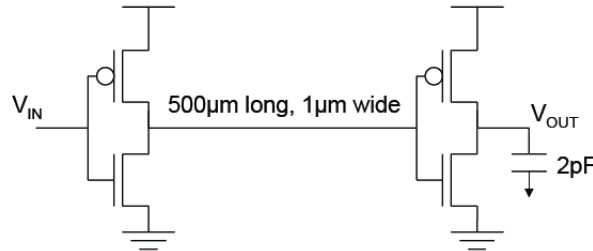
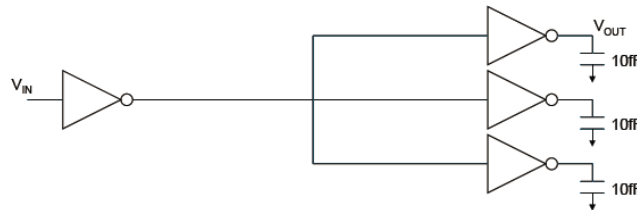


1. (a). What is the delay from  $V_{IN}$  to  $V_{OUT}$  in the following circuit. Assume that the wire resistance is  $0.06 \Omega/\square$  and the wire capacitance is  $0.07 \text{ fF}/\mu\text{m}^2$ . The equivalent resistance for the NMOS and PMOS transistors are  $13 \text{ k}\Omega$  and  $31 \text{ k}\Omega$  respectively. Assume that the input capacitance is  $5 \text{ fF}$  for a minimum sized transistor.

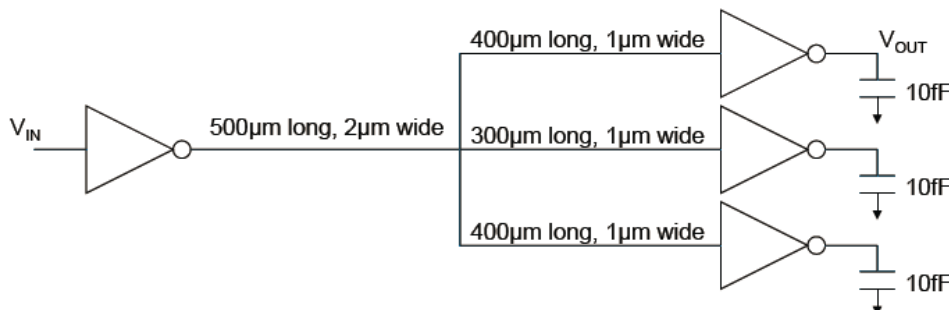


- (b). If you scale the second inverter by a factor of 2, what happens to the delay time? Note that scaling the second inverter will decrease its equivalent resistance and increase its intrinsic capacitance.  
(c) If you keep on scaling the second inverter, what trends do you expect to observe for the delay? Explain qualitatively.

2. Given the following circuit, estimate the delay time from  $V_{IN}$  to  $V_{OUT}$ . For all inverters, the equivalent resistance is  $10 \text{ k}\Omega$ , and the input capacitance of each inverter is  $10 \text{ fF}$ . (hint: use Elmore delay model)

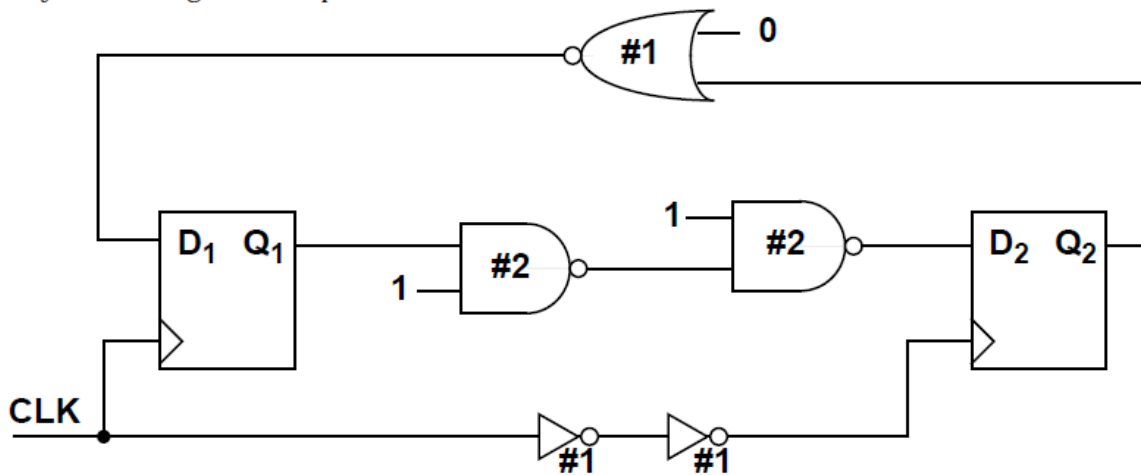


3. Given the following circuit, estimate the delay time from  $V_{IN}$  to  $V_{OUT}$ . For all inverters, the equivalent resistance is  $10 \text{ k}\Omega$ , and the input capacitance of each inverter is  $10 \text{ fF}$ . The wire resistance is  $0.06 \Omega/\square$  and the wire capacitance is  $0.07 \text{ fF}/\mu\text{m}^2$ .

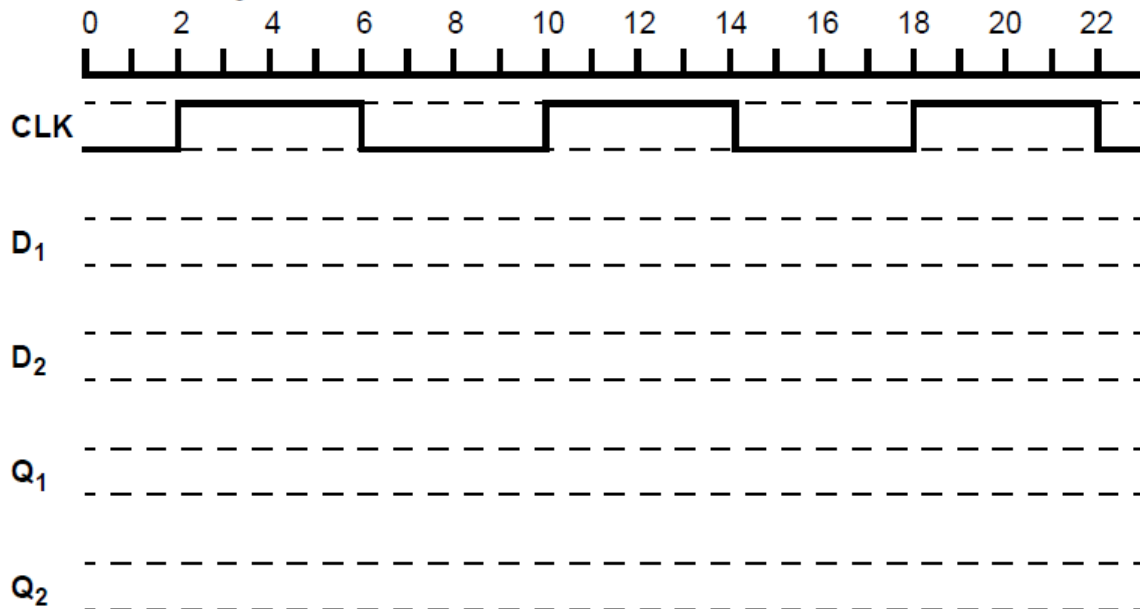


#### 4. Pipelines I: Timing

The circuit shown below uses two identical rising edge triggered Flip-Flops. Assume that for both Flip-Flops, the *setup time* is one time unit, the *propagation delay* is one time unit, and the *hold time* is two time units. The gates, buffers and inverters in this circuit are annotated with their propagation delays in the same time units. Assume that maximum and minimum propagation delays for these gates are equivalent.



- A. Complete the following timing diagram for the circuit. Assume the initial states of  $Q_1$  and  $Q_2$  are 0, and have remained at 0 for a long time (but no clock edge has come along yet to latch the 1 value at  $D_1$ ).



- B. What is the *minimum clock period* of this circuit that will assure that it works? Describe the critical path.