

Computational Intelligence Lecture 9: Designing Controller Using Neural Networks

Farzaneh Abdollahi

Department of Electrical Engineering

Amirkabir University of Technology

Lecture 9

Open-Loop Inverse Dynamics

NN in Control Feedback Gradient Through Plant Gradient Through The Model of The Plant

Adaptive Control Using Neural Networks

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Open-Loop Inverse Dynamics

- The Inverse model obtained from identification is directly applied.
- ► ∴ Considering reference signal r

$$y = f^{-1}fr = r$$

 This method can be considered as Indirect adaptive control



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NN in Control Feedback



- Objective: Tracking reference signal r
- But: In this model, output of NN for training is not available ~> BP can not be applied directly.

$$e = r - y, \quad E = \frac{1}{2}e^2$$

 $\bigtriangleup w_{ij} = -\eta \frac{\partial E}{\partial w_{ij}}$

• Only output of the plant, y is available.





Gradient Through Plant



The plant can be considered as output layer of NN with fixed weights

▶ ∴ desired output of the NN is available and BP algorithm can be employed.

$$\frac{\partial E}{\partial w_{ij}} = \frac{\partial E}{\partial e} \cdot \frac{\partial e}{\partial y} \cdot \frac{\partial y}{\partial w_{ij}}$$
$$\frac{\partial E}{\partial e} = e, \quad \frac{\partial e}{\partial y} = -1$$
$$\frac{\partial y}{\partial w_{ij}} = \frac{\partial y}{\partial u} \cdot \frac{\partial u}{\partial w_{ij}}$$

► To train the NN, $\frac{\partial y}{\partial u}$ is required, therefore, this method is so-called Gradient through plant

NN in Control Feedback



- If the plant dynamics is not known $\frac{\partial y}{\partial u}$ is not available!!
- Solution
 - 1. Using a NN identifier to identify the system dynamics directly.
 - Then apply $\frac{\partial \hat{y}}{\partial u}$ instead of $\frac{\partial y}{\partial u}$.
 - This method is so-called Gradient Through The Model of The Plant
 - 2. Approximate $\frac{\partial y}{\partial u}$ with $sign\{\frac{\partial y}{\partial u}\}$ which is usually available without knowing the dynamics
 - If the direction of the gradient is true, the magnitude of ∂y/∂u can be compensated by η



Adaptive Control Using Neural Networks

1. Direct Control

 Parameters of the controller is directly adjusted to reduce the norm of output error



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Adaptive Control Using Neural Networks

2. Indirect Control

The model of the plant is identified first and the parameters of the controller is defined based on identified model



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▶ They can be a neural networks controller



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Example [1]

- ► Consider the difference equation: y_p(k + 1) = f[y_p(k), y_p(k - 1)] + u(k)
- ► f(.) is unknown
- For the sake of simulation $f[y_p(k), y_p(k-1)] = \frac{y_p(k)y_p(k-1)[y_p(k)+2.5]}{1+y_p^2(k)+y_p^2(k-1)}$
- ► Reference model: $y_m(k+1) = 0.6y_m(k) + 0.2y_m(k-1) + r(k)$
- $r(k) = sin(\frac{2\pi k}{25})$: a bounded reference input
- ► Objective: Determine a bound control signal u(k) s.t. $\lim_{k\to\infty} e_c(k) = y_p(k) - y_m(k) = 0$

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- ▶ If f(.) was known the proper control signal would be $u(k) = -f[y_p(k), y_p(k-1)] + 0.6y_p(k) + 0.2y_p(k-1) + r(k)$ yields $e_c(k+1) = 0.6e_c(k) + 0.2e_c(k-1)$
 - \therefore the reference model is a.s. since $\lim_{k\to\infty} e_c(k) = 0$
- Since the plant is unknown, assuming the unforced system is stable, f(.) is estimated by series parallel NN identifier as f̂(.)
- Hence $u(k) = -\hat{f}[y_p(k), y_p(k-1)] + 0.6y_p(k) + 0.2y_p(k-1) + r(k)$

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- Identification will be off-line
- Once the plant is identified in desired level of accuracy, control is initiated to make the plant output follow the reference model.
- Note that using the estimated function in fb loop may result in unbounded solution
- Hence for on-line control, identification and control should proceed simultaneously.
- ► The time interval *T_i* and *T_c* for updating the identification and control parameters should be chosen wisely.

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- ▶ a) Identified signal \hat{y}_p (dashed) and output of the plant with no control action (solid)
- b) Response for r = sin(^{2πk}/₂₅) with control (dashed); reference signal (solid)
- $T_i = T_c = 1$





- Choose $T_i = T_c = 10$
- Response for $r = sin(\frac{2\pi k}{25})$ with control (dashed); reference signal (solid)
- ► ∴ To have stable on-line control, the identification should be accurate enough before the control action is initiated!



Example 2 [1]

- Consider the difference equation: y_p(k+1) = f[y_p(k), y_p(k-1), ..., y_p(k-n+1)] + ∑_{j=0}^{m-1} β_ju(k-j) m ≤ n
 f(.) and β_i are unknown; β₀ is nonzero with known sign
- ► For the sake of simulation $f[y_p(k), y_p(k-1)..., y_p(k-n+1)] = \frac{5y_p(k)y_p(k-1)}{1+y_p^2(k)+y_p^2(k-1)+y_p^2(k-2)};$ $\beta_0 = 1, \beta_1 = 0.8$
- ► Reference model: $y_m(k+1) = 0.32y_m(k) + 0.64y_m(k-1) - 0.5y_m(k-2) + r(k)$
- $r(k) = sin(\frac{2\pi k}{25})$: a bounded reference input
- ► Objective: Determine a bound control signal u(k) s.t. lim_{k→∞} e_c(k) = y_p(k) - y_m(k) = 0
- Assume $sgn(\beta_0) = +1; \beta_0 \ge 0.1$

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- The control signal is: $u(k) = \frac{1}{\hat{\beta}_0} [-\hat{f}_k[y_p(k), y_p(k-1), y_p(k-2)] \hat{\beta}_1 u(k-1) + 0.32y_p(k) + 0.64y_p(k-1) 0.5y_p(k-2) + r(k)]$
- Choose $T_i = T_c = 10$
- ► Response for r = sin(^{2πk}/₂₅) with control (dashed); reference signal (solid) left): first 100 sec; right) after 9900sec



Example 3 [1]

- Consider dynamics similar to Example 2 but replace 0.8u(k-1) with $\frac{1.1u(k-1)}{2}$
- Apply similar controller
- ▶ The system is nonminimum phase (it has zero out of unit circle)
- ▶ ∴ The output error is bounded but the control signal is unbounded

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- ▶ left) Response for $r = sin(\frac{2\pi k}{25})$ with control (dashed); reference signal (solid)
- right) control signal u(k)



Inverse Dynamics Model Learning (IDML) [2]

- Consider the system dynamics $\ddot{x} = f(x, \dot{x}) + u$, y = x
- ▶ To track reference signal y_a , control signal can be defined $u = u_n + u_c$
 - $u_c = (-\ddot{y}_a) + K_1(\dot{y}_r \dot{y}_a) + K_0(y_r y_a)$ is conventional FB controller • $u_n = -f(x, \dot{x})$
- f(.) is not known and is estimated by NN $\rightsquigarrow u_n = \hat{f}$

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- The error signal for training is $e_n = u u_n = u_c$
- The learning rule is $\dot{w} = \eta \frac{\partial \hat{f}}{\partial w} u_c$



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Example 4 [2]

• Consider one-link flexible arm: $M(\delta) \begin{bmatrix} \dot{\theta} \\ \ddot{\delta} \end{bmatrix} + \begin{bmatrix} h_1(\dot{\theta}, \delta, \dot{\delta}) + F_1 \dot{\theta} + f_c \\ h_2(\dot{\theta}, \delta) + K\delta + F_2 \dot{\delta} \end{bmatrix} = \begin{bmatrix} u \\ 0 \end{bmatrix}$

- θ : hub angle
- δ: deflection variable
- h_1 and h_2 are Coriolis and Centrifugal forces, respectively
- M(δ): P.D. inertia matrix
- ► *u*: torque
- ► *F*₁: viscus damping; *F*₂ damping matrix;
- *f_c* hub friction; *K* stiffness matrix

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- > The nonlinear dynamics is assumed to be unknown
- ▶ For the sake of simulation, the numerical values are

$$M(\delta) = \begin{bmatrix} m(\delta) & 1.0703 & -0.0282 \\ 1.0703 & 1.6235 & -0.4241 \\ -0.0282 & -0.4241 & 2.592 \end{bmatrix}; \\ m(\delta) = 0.9929 + 0.12(\delta_1^2 + \delta_2^2) - 0.24\delta_1\delta_2 \\ \mathbf{k} = \begin{bmatrix} 17.4561 & 0 \\ 0 & 685.5706 \end{bmatrix} \\ \mathbf{h}_1(\dot{\theta}, \delta, \dot{\delta}) = 0.24\dot{\theta}[(\delta_1 - \delta_2)\dot{\delta}_1 - (\delta_1 - \delta_2)\dot{\delta}_2] \\ \mathbf{h}_2(\dot{\theta}, \delta) = \begin{bmatrix} -0.12\dot{\theta}^2(\delta_1 - \delta_2) \\ -0.12\dot{\theta}^2(\delta_2 - \delta_1) \end{bmatrix} \\ \mathbf{k} = f_c = C_{coul}(\frac{2}{1+e^{-10\theta}} - 1); \ C_{coul} = \begin{cases} 4.74 & \dot{\theta} > 0 \\ 4.77 & \dot{\theta} < 0 \end{cases}$$

▶ By output redefinition, the nonminimum phase problem is solved

- The NN structure:
 - Three layer: 4 input; 5 hidden,1 output
- $K_0 = 1; K_1 = 2$

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to sin(t) reference trajectory using the Figure 4.7: Output Lecture 9 Neural Networks

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igure 4.8: Actual tip responses to step input for System II using the IDML neural etwork controller; (dashed line corresponds to model with Coulomb friction at the ub).

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