

# Computational Intelligence **Lecture 8: Designing Controller Using Neural Networks**

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Neural Networks Lecture 8 1/26



Open-Loop Inverse Dynamics

NN in Control Feedback
Gradient Through Plant
Gradient Through The Model of The Plant

Adaptive Control Using Neural Networks



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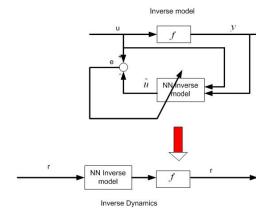


### Open-Loop Inverse Dynamics

- The Inverse model obtained from identification is directly applied.
- ► ∴ Considering reference signal r

$$y = f^{-1}fr = r$$

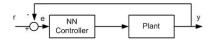
This method can be considered as Indirect adaptive control



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### NN in Control Feedback



- Objective: Tracking reference signal r
- ▶ But: In this model, output of NN for training is not available → BP can not be applied directly.

$$e = r - y, \quad E = \frac{1}{2}e^{2}$$
  
$$\triangle w_{ij} = -\eta \frac{\partial E}{\partial w_{ij}}$$

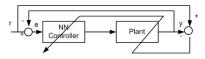
▶ Only output of the plant, y is available.

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## Gradient Through Plant



- ► The plant can be considered as output layer of NN with fixed weights
- ▶ ∴ desired output of the NN is available and BP algorithm can be employed.

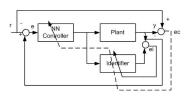
$$\begin{split} \frac{\partial E}{\partial w_{ij}} &= \frac{\partial E}{\partial e} \cdot \frac{\partial e}{\partial y} \cdot \frac{\partial y}{\partial w_{ij}} \\ \frac{\partial E}{\partial e} &= e, \quad \frac{\partial e}{\partial y} = -1 \\ \frac{\partial y}{\partial w_{ii}} &= \frac{\partial y}{\partial u} \cdot \frac{\partial u}{\partial w_{ij}} \end{split}$$

► To train the NN,  $\frac{\partial y}{\partial u}$  is required, therefore, this method is so-called Gradient through plant

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### NN in Control Feedback



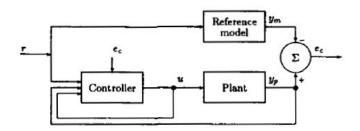
- ▶ If the plant dynamics is not known  $\frac{\partial y}{\partial u}$  is not available!!
- Solution
  - 1. Using a NN identifier to identify the system dynamics directly.
    - ► Then apply  $\frac{\partial \hat{y}}{\partial u}$  instead of  $\frac{\partial y}{\partial u}$ .
    - ► This method is so-called Gradient Through The Model of The Plant
  - 2. Approximate  $\frac{\partial y}{\partial u}$  with  $sign\{\frac{\partial y}{\partial u}\}$  which is usually available without knowing the dynamics
    - If the direction of the gradient is true, the magnitude of  $\frac{\partial y}{\partial u}$  can be compensated by  $\eta$

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# Adaptive Control Using Neural Networks

### 1. Direct Control

 Parameters of the controller is directly adjusted to reduce the norm of output error





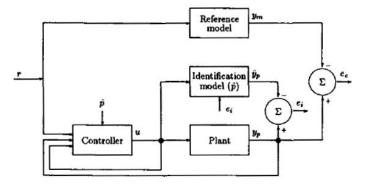
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### Adaptive Control Using Neural Networks

### 2. Indirect Control

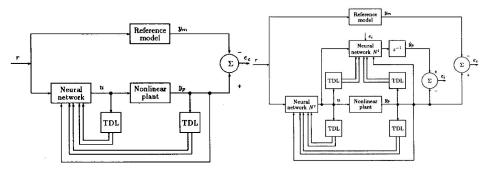
▶ The model of the plant is identified first and the parameters of the controller is defined based on identified model



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▶ They can be a neural networks controller



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# Example [1]

► Consider the difference equation:

$$y_p(k+1) = f[y_p(k), y_p(k-1)] + u(k)$$

- ightharpoonup f(.) is unknown
- ► For the sake of simulation  $f[y_p(k), y_p(k-1)] = \frac{y_p(k)y_p(k-1)[y_p(k)+2.5]}{1+y_p^2(k)+y_p^2(k-1)}$
- ► Reference model:  $y_m(k+1) = 0.6y_m(k) + 0.2y_m(k-1) + r(k)$
- ▶  $r(k) = sin(\frac{2\pi k}{25})$ : a bounded reference input
- ▶ Objective: Determine a bound control signal u(k) s.t.  $\lim_{k\to\infty} e_c(k) = y_p(k) y_m(k) = 0$



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- ▶ If f(.) was known the proper control signal would be  $u(k) = -f[y_p(k), y_p(k-1)] + 0.6y_p(k) + 0.2y_p(k-1) + r(k)$  yields  $e_c(k+1) = 0.6e_c(k) + 0.2e_c(k-1)$ 
  - : the reference model is a.s. since  $\lim_{k\to\infty} e_c(k) = 0$
- $\triangleright$  Since the plant is unknown, assuming the unforced system is stable, f(.)is estimated by series parallel NN identifier as  $\hat{f}(.)$
- ► Hence  $u(k) = -\hat{f}[y_p(k), y_p(k-1)] + 0.6y_p(k) + 0.2y_p(k-1) + r(k)$

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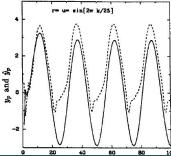


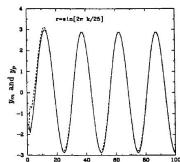
- ▶ Identification will be off-line
- ▶ Once the plant is identified in desired level of accuracy, control is initiated to make the plant output follow the reference model.
- Note that using the estimated function in fb loop may result in unbounded solution
- Hence for on-line control, identification and control should proceed simultaneously.
- ▶ The time interval  $T_i$  and  $T_c$  for updating the identification and control parameters should be chosen wisely.

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- $\triangleright$  a) Identified signal  $\hat{y}_p$  (dashed) and output of the plant with no control action (solid)
- **b**) Response for  $r = sin(\frac{2\pi k}{25})$  with control (dashed); reference signal (solid)
- $ightharpoonup T_i = T_c = 1$





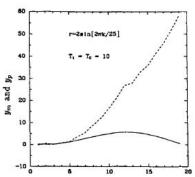
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- ightharpoonup Choose  $T_i = T_c = 10$
- ► Response for  $r = sin(\frac{2\pi k}{25})$  with control (dashed); reference signal (solid)
- ▶ ∴ To have stable on-line control, the identification should be accurate enough before the control action is initiated!



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# Example 2 [1]

► Consider the difference equation:

$$y_p(k+1) = f[y_p(k), y_p(k-1), ..., y_p(k-n+1)] + \sum_{j=0}^{m-1} \beta_j u(k-j) \ m \le n$$

- ▶ f(.) and  $\beta_j$  are unknown;  $\beta_0$  is nonzero with known sign
- ► For the sake of simulation  $f[y_p(k), y_p(k-1)..., y_p(k-n+1)] = \frac{5y_p(k)y_p(k-1)}{1+y_p^2(k)+y_p^2(k-1)+y_p^2(k-2)};$  $\beta_0 = 1, \beta_1 = 0.8$
- ► Reference model:

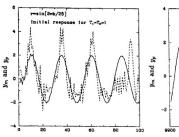
$$y_m(k+1) = 0.32y_m(k) + 0.64y_m(k-1) - 0.5y_m(k-2) + r(k)$$

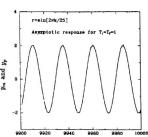
- ▶  $r(k) = sin(\frac{2\pi k}{25})$ : a bounded reference input
- ▶ Objective: Determine a bound control signal u(k) s.t.  $\lim_{k\to\infty} e_c(k) = y_p(k) y_m(k) = 0$
- Assume  $sgn(\beta_0) = +1; \beta_0 \ge 0.1$





- ► The control signal is:  $u(k) = \frac{1}{\hat{\beta}_0} [-\hat{f}_k[y_p(k), y_p(k-1), y_p(k-2)] \hat{\beta}_1 u(k-1) + 0.32y_p(k) + 0.64y_p(k-1) 0.5y_p(k-2) + r(k)]$
- ► Choose  $T_i = T_c = 10$
- ► Response for  $r = sin(\frac{2\pi k}{25})$  with control (dashed); reference signal (solid) left): first 100 sec; right) after 9900sec







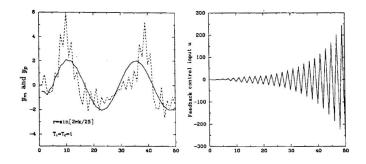
# Example 3 [1]

- ► Consider dynamics similar to Example 2 but replace 0.8u(k-1) with 1.1u(k-1)
- ► Apply similar controller
- ▶ The system is nonminimum phase (it has zero out of unit circle)
- ▶ ∴ The output error is bounded but the control signal is unbounded

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- left) Response for  $r = sin(\frac{2\pi k}{25})$  with control (dashed); reference signal (solid)
- ightharpoonup right) control signal u(k)



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# Inverse Dynamics Model Learning (IDML) [2]

- ▶ Consider the system dynamics  $\ddot{x} = f(x, \dot{x}) + u$ , y = x
- lacktriangle To track reference signal  $y_a$ , control signal can be defined  $u=u_n+u_c$

• 
$$u_c = (-\ddot{y}_a) + K_1(\dot{y}_r - \dot{y}_a) + K_0(y_r - y_a)$$
 is conventional FB controller

$$u_n = -f(x, \dot{x})$$

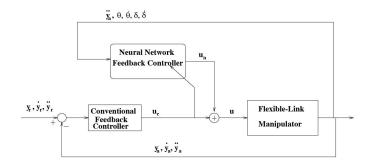
▶ f(.) is not known and is estimated by NN  $\leadsto u_n = \hat{f}$ 



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- ▶ The error signal for training is  $e_n = u u_n = u_c$
- lacktriangle The learning rule is  $\dot{w}=\eta rac{\partial \hat{f}}{\partial w}u_c$



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# Example 4 [2]

► Consider\_one-link flexible\_arm:

$$M(\delta) \begin{bmatrix} \ddot{\theta} \\ \ddot{\delta} \end{bmatrix} + \begin{bmatrix} h_1(\dot{\theta}, \delta, \dot{\delta}) + F_1\dot{\theta} + f_c \\ h_2(\dot{\theta}, \delta) + K\delta + F_2\dot{\delta} \end{bmatrix} = \begin{bmatrix} u \\ 0 \end{bmatrix}$$

- $\blacktriangleright$   $\theta$ : hub angle
- $\delta$ : deflection variable
- $\blacktriangleright$   $h_1$  and  $h_2$  are Coriolis and Centrifugal forces, respectively
- $M(\delta)$ : P.D. inertia matrix
- u: torque
- ► F<sub>1</sub>: viscus damping; F<sub>2</sub> damping matrix;
- ▶ f<sub>c</sub> hub friction; K stiffness matrix

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- ► The nonlinear dynamics is assumed to be unknown
- ▶ For the sake of simulation, the numerical values are

$$\begin{split} & \blacktriangleright \ M(\delta) = \begin{bmatrix} m(\delta) & 1.0703 & -0.0282 \\ 1.0703 & 1.6235 & -0.4241 \\ -0.0282 & -0.4241 & 2.592 \end{bmatrix}; \\ & m(\delta) = 0.9929 + 0.12(\delta_1^2 + \delta_2^2) - 0.24\delta_1\delta_2 \\ & \blacktriangleright \ K = \begin{bmatrix} 17.4561 & 0 \\ 0 & 685.5706 \end{bmatrix} \\ & \blacktriangleright \ h_1(\dot{\theta}, \delta, \dot{\delta}) = 0.24\dot{\theta}[(\delta_1 - \delta_2)\dot{\delta}_1 - (\delta_1 - \delta_2)\dot{\delta}_2] \\ & \blacktriangleright \ h_2(\dot{\theta}, \delta) = \begin{bmatrix} -0.12\dot{\theta}^2(\delta_1 - \delta_2) \\ -0.12\dot{\theta}^2(\delta_2 - \delta_1) \end{bmatrix} \\ & \blacktriangleright \ f_c = C_{coul}(\frac{2}{1+e^{-10\dot{\theta}}} - 1); \ C_{coul} = \begin{cases} 4.74 & \dot{\theta} > 0 \\ 4.77 & \dot{\theta} < 0 \end{cases} \end{split}$$

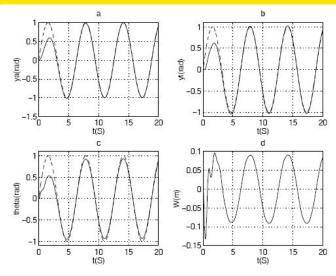
▶ By output redefinition, the nonminimum phase problem is solved

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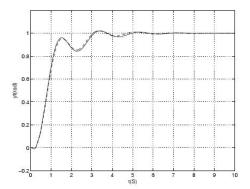
- ► The NN structure:
  - ► Three layer: 4 input; 5 hidden,1 output
- $K_0 = 1; K_1 = 2$

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igure 4.8: Actual tip responses to step input for System II using the IDML neural etwork controller; (dashed line corresponds to model with Coulomb friction at the ub).



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## References



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